

## Background gas analysis with leaky attenuation in ball surface acoustic wave trace moisture analyzer

ボール SAW 微量水分計における漏洩減衰を用いたバックグラウンドガスの分析

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### 1. Introduction

In trace moisture analyzers (TMA), not only the moisture but also composition of background gas (BG) is sometimes required. As an example, hydrogen concentration ( $[H_2]$ ) is required when hydrogen is introduced in NG for transport purpose. In moisture purge of a clean chamber using a purge gas, local concentration measurement of the purge gas is useful to optimize the purge process.

We have developed the ball SAW TMA with two frequency measurement (TFM) of delay time to compensate temperature variation as well as to measure the temperature. In this work, we extend these works to the TFM of amplitude to measure the composition of BG, as well as to compensate the variation of BG.

### 2. Principle

In a SAW sensor, burst of two frequency  $f_1$  and  $f_2$  is transmitted and attenuation  $\alpha_1$  and  $\alpha_2$  at each frequency is measured. The attenuations are given by

$$\alpha_1 = a_0 F_1 + a_1(w) F_1^2 + a_2 F_1^y \quad (1)$$

$$\alpha_2 = a_0 F_2 + a_1(w) F_2^2 + a_2 F_2^y \quad (2)$$

where  $F_1 = f_1 / f_0$ ,  $F_2 = f_2 / f_0$ ,  $f_0$  is a reference frequency.

$$a_0 = \alpha_L l = \frac{f_0 P l}{\rho_s V_s^2} \sqrt{\frac{\gamma M}{RT}} \quad (3)$$

is an attenuation caused by a leakage to the background gas at frequency  $f_0$ , where  $l$  is the SAW propagation distance,  $\rho_s, V_s$  are density and SAW velocity of substrate,  $P$  is pressure,  $R$  is gas constant,  $T$  is temperature,  $M$  is molecular weight,  $\gamma$  is ratio of specific heat at constant pressure to specific heat at constant volume.  $a_1(w)$  is a viscoelastic loss by moisture,  $w$  is moisture concentration,  $a_2$  is a device loss due to

scattering at electrodes, etc, and  $y$  is a frequency dependence index of the device loss.

A leakage factor is defined as

$$\Delta \alpha_L \equiv \left[ (f_2 / f_1)^2 \alpha_1 - \alpha_2 \right] / l \quad (4),$$

and from eqs. (1) and (2), it is given by

$$\Delta \alpha_L = \alpha_L (F_1^{-1} F_2^2 - F_2) + (a_2 / l) (F_1^{y-2} F_2^2 - F_2^y) \quad (5)$$

Similarly, viscoelastic factor is defined and given by

$$\Delta \alpha_V = \left[ \alpha_2 - (F_2 / F_1) \alpha_1 \right] / l \quad (6)$$

$$= [a_1(w) / l] (F_2^2 - F_1 F_2) + (a_2 / l) (F_2^y - F_1^{y-1} F_2)$$

In a special case of  $F_2 = 3F_1$ ,  $F_1 = 1$ ,

$$\Delta \alpha_L = 6\alpha_L + (a_2 / l) (9 - 3^y) \quad (7)$$

$$\Delta \alpha_V = 6[a_1(w) / l] + (a_2 / l) (3^y - 3)$$

Using eqs. (3), (7), a gas parameter is given by

$$G \equiv \sqrt{\gamma M} = B \left[ \Delta \alpha_L - (a_2 / l) (9 - 3^y) \right] \quad \text{where}$$

$$B = \left( \rho_s V_s^2 \sqrt{RT} \right) / (6 f_0 P) \quad (8)$$

### 2. Experiment

In a humid gas with a frost point of  $-60^\circ\text{C}$  (10.7 ppmv), the background gas was changed from Air,  $N_2$ , Ar to  $CH_4$  as shown in **Fig. 1**. The attenuations  $\alpha_1$ ,  $\alpha_2$  and the leakage factor  $\Delta \alpha_L$  were measured, as plotted in **Fig. 2** and **Fig. 3**. Using the known value of gas parameter  $G$  for  $N_2$  and Ar, the coefficient  $B$  and the term caused by device loss were calibrated as  $B = 0.1085$  and  $(a_2 / l) (9 - 3^y) = 58.53$  dB/m. When  $T$  and  $P$  are changed, these values should be recalibrated using independent measurement of  $T, P$ .

Assuming that the first and the fourth background gases in Figs. 2 and 3 are unknown, we measured the gas parameter  $G^*$  as 4.43 and 6.36 using eq. (8). We note that they are most close to

4.56 of CH<sub>4</sub> and 6.35 of Air as shown in Table I.

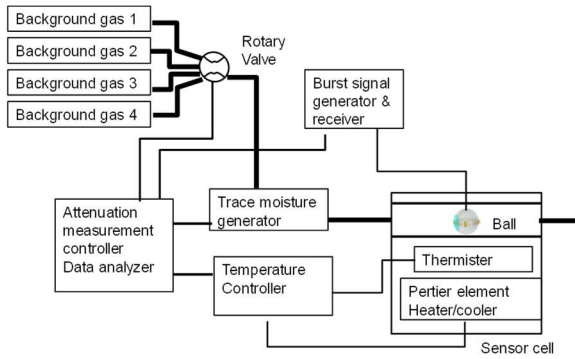


Fig.1 Experimental setup

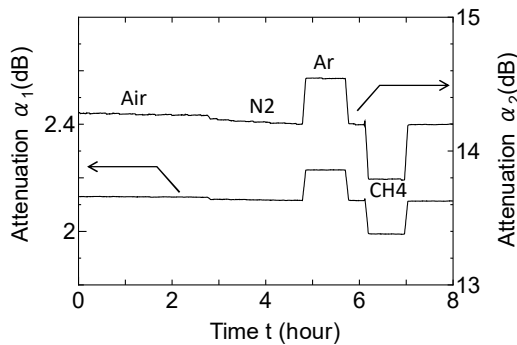


Fig. 2 Attenuation at 80MHz and 240 MHz

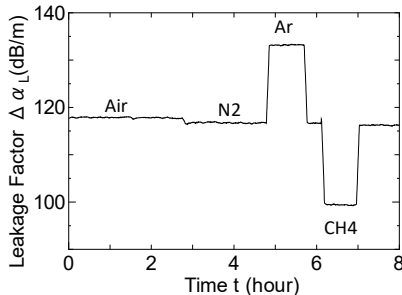


Fig. 3 Variation of leakage factor

Background gas	Molecular weight $M$	Heat capacity ratio $\gamma$	Gas parameter $\sqrt{\gamma M}$
CH <sub>4</sub>	16	1.30	4.56
N <sub>2</sub>	28	1.40	6.26
Air	28.8	1.40	6.35
Ar	40	1.67	8.17

Table I. Parameters of background gases

At another frost point of -50°C (38.8 ppmv), the background gas was changed four times, and the leakage factor was measured. Since they were very close to 6.26, 8.17, 4.56 and 6.35 of N<sub>2</sub>, Ar, CH<sub>4</sub> and Air, they are estimated to be these gasses. The measurement error was less than 2.7%. The measured and true gas parameter for all the experiment is summarized in Fig. 4. The agreement between measured and true  $G$  is significant.

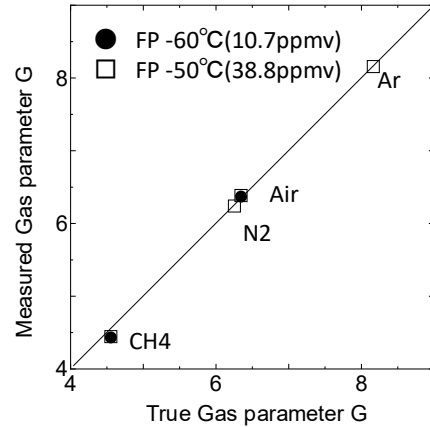


Fig.4 Comparison of measured and true values of Gas parameter.

In a mixed gas, we propose that an average gas parameter is given by

$$\bar{G} = \sqrt{\bar{\gamma} \bar{M}} = \sqrt{(C_p / C_v) \bar{M}} \quad (9)$$

where  $\bar{M}$  is average molecular constant and  $\bar{\gamma}$  is average ratio of specific heat at constant pressure  $C_p$  to specific heat at constant volume  $C_v$ . For mixed gases of He and N<sub>2</sub>, the measured gas parameter is plotted against the molar fraction of He in Fig. 5. Since they agreed to the calculated value, eq. (9) was verified. Thus, it is possible to measure He molar fraction from measured gas parameter.

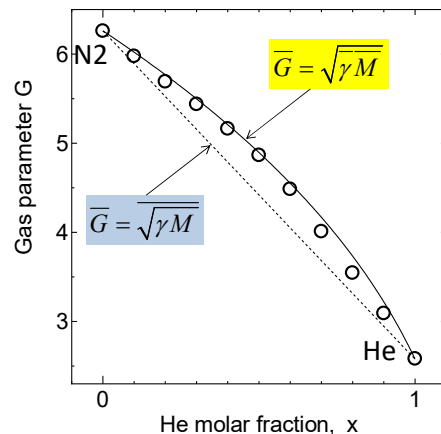


Fig. 5 Gas parameter against He molar fraction

### Conclusions

A method of background gas analysis with leaky attenuation in ball SAW sensor was proposed and the accuracy of the proposed method was verified.

### References

1. K. Yamanaka, et al., IEEE Trans. on UFFC, 53 (2006) 793.
2. A. J. Slobodnik, Jr., J. Appl. Phys., 43 (1972) 2565.